

No Calculator. Show your work in details.

1. (1pt) State the definitions of  $f'(x)$ .

$$f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h} \text{ provided the limit exists.}$$

2. (1pt) Let  $r$  be a real number.  $\frac{d}{dx}[x^r] = rx^{r-1}$

3. (8pts) Compute  $h'(x)$  (without using the Product Rule and Quotient Rule). It is not required to simply the answers.

$$(1) h(x) = x^{2017} + \frac{1}{x^{2017}} - 2\sqrt[3]{x} + \frac{1}{\sqrt{x}} - e^x + e^3 + \sqrt{2}$$

$$h(x) = x^{2017} + x^{-2017} - 2x^{1/3} + x^{-1/2} - e^x + e^3 + \sqrt{2}$$

$$\begin{aligned} h'(x) &= 2017x^{2-16} - 2017x^{-2018} - \frac{2}{3}x^{-2/3} - \frac{1}{2}x^{-3/2} + e^x + 0 + 0 \\ &= 2017x^{2-16} - 2017x^{-2018} - \frac{2}{3}x^{-2/3} - \frac{1}{2}x^{-3/2} + e^x \end{aligned}$$

$$(2) h(x) = (2x^2 - x)(x^3 - 3)$$

$$h(x) = 2x^5 - x^4 - 6x^2 + 3x$$

$$h'(x) = 10x^4 - 4x^3 - 12x + 3$$

$$(3) h(x) = \frac{\sqrt{x} + 3 - x}{x^2}$$

$$h(x) = x^{-3/2} + 3x^{-2} - x^{-1}$$

$$h'(x) = -\frac{3}{2}x^{-5/2} - 6x^{-3} + x^{-2}$$